

X-ray data booklet (<http://xdb.lbl.gov/xdb-new.pdf>)

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1.7 atomic scattering factors

1.6 mass absorption coefficients

index of refraction

$$\begin{aligned} n &= 1 - \delta - i \cdot \beta \\ &= 1 - \frac{r_e}{\lambda^2} \cdot \sum_j N(j) \cdot f(j) \end{aligned} \quad (1.7.1)$$

δ	refractive index decrement (RID)
β	absorption index
r_e	classical electron radius = $2.817940289458 \times 10^{-15}$ [m]
λ	wave length
$N(j)$	number of element "j" per unit volume
$f(j)$	atomic scattering factor of element "j"

$$\lambda \text{ [m]} = (h \cdot c / e) / E \text{ [eV]} = 1.239841576558181422983 \times 10^{-6} / E \text{ [eV]}$$

h	Planck constant = $6.6260689633 \times 10^{-34}$ [J · s]
c	speed of light = 2.99792458×10^8 [m / s]
e	electron charge = $1.6021768740 \times 10^{-19}$ [C]
$E \text{ [eV]}$	photon energy in eV

$$N(j) = n_a \cdot \rho \cdot w(j) / A(j)$$

n_a	Avogadro's number = $6.0221417930 \times 10^{23}$ [1 / mol]
ρ	density of material (including element "j")
$w(j)$	weight ratio of element "j"
$A(j)$	atomic weight of element "j"

$$f(j) = f_1(j) + i \cdot f_2(j) \quad (1.7.2)$$

http://henke.lbl.gov/optical_constants/sf/sf.tar.gz

RID

$$\delta = \rho \cdot n_a \cdot r_e / \lambda^2 \cdot \sum_j w(j) \cdot f_1(j) / A(j)$$

atomic mass RID (MRID)

$$\Delta(j) = n_a \cdot r_e / \lambda^2 \cdot f_1(j) / A(j)$$

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$$\delta = \rho \cdot \sum_j w(j) \cdot \Delta(j)$$

absorption index

$$\beta = \rho \cdot n_a \cdot r_e / \lambda^2 \cdot \sum_j w(j) \cdot f_2(j) / A(j)$$

atomic photo-absorption cross section

$$\sigma(j) = 2 \cdot r_e \cdot \lambda \cdot f_2(j) \quad (1.7.3)$$

atomic mass photo-absorption coefficients (MPAC)

$$\begin{aligned} \tau(j) &= n_a \cdot \sigma(j) / A(j) \\ &= n_a \cdot 2 \cdot r_e \cdot \lambda \cdot f_2(j) / A(j) \end{aligned} \quad (1.6.2)$$

linear photo-absorption coefficients (LPAC)

$$\begin{aligned} \mu &= \rho \cdot \sum_j w(j) \cdot \tau(j) \\ &= (4 \cdot \pi / \lambda) \cdot \beta \end{aligned} \quad (1.6.3)$$